



Unified International
Mathematics Olympiad

UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD (UPDATED)

CLASS - 8

Question Paper Code : 4P104

KEY

1	2	3	4	5	6	7	8	9	10
C	D	A	D	B	C	C	B	C	C
11	12	13	14	15	16	17	18	19	20
C	B	A	D	C	B	C	B	C	B
21	22	23	24	25	26	27	28	29	30
A	A	D	D	C	B	A	D	B	B
31	32	33	34	35	36	37	38	39	40
A,B,C,D	A,B,C	B,C,D	A,C	A,B,D	D	C	B	C	B
41	42	43	44	45	46	47	48	49	50
A	A	C	B	A	Del	A	C	A	D

SOLUTIONS

MATHEMATICS - 1 (MCQ)

01. (C) $\sqrt{1^3 + 2^3 + 3^3 + \dots + 9^3} = \sqrt{2025} = 45$

02. (D) $\sqrt[3]{100^3 - 3 \times 100^2 \times 97 + 3 \times 100 \times 97^2 - 97^3}$
 $= \sqrt[3]{(100 - 97)^3} = 3$

03. (A) Given $P \left(1 + \frac{R}{100}\right)^2 - P - \frac{PTR}{100} = \text{Rs. } 1.5$

$$P \left(1 + \frac{5}{100}\right)^2 - P = \frac{P \times 2 \times 5}{100} = \text{Rs. } 1.5$$

$$\frac{441P}{400} - P - \frac{P}{10} = \text{Rs. } 1.5$$

$$\frac{441P - 400P - 40P}{400} = \text{Rs. } 1.5$$

$$\frac{P}{400} = \text{Rs. } 1.5 \Rightarrow P = \text{Rs. } 600$$

04. (D) Originally, let there be x men. Less men
 \Rightarrow more days.

$$\therefore (x - 10) : x :: 100 : 110$$

$$\Rightarrow (x - 10) \times 110 = x \times 100$$

$$\Rightarrow 10x = 1100 \Rightarrow x = 110$$

05. (B) Let the cost of pressure cooker be Rs x . & sales be y .

\therefore Total amount = Rs xy .

$$\text{Given new cost} = 80\% x = \frac{80}{100} x = \frac{4x}{5}$$

$$\text{New sales} = 180\% y = \frac{180}{100} y = \frac{9}{5} y$$

$$\text{New amount} = \frac{4x}{5} \times \frac{9}{5} = \frac{36xy}{25}$$

$$\text{Increased sales} = \frac{36xy}{25} - xy = \frac{11xy}{25}$$

Increased sales %

$$= \frac{\left(\frac{11xy}{25}\right)}{xy} \times 100 = \frac{(11)}{25} \times 100$$

$$= 44\%$$

06. (C) Let x be a number. Then the other two numbers are $2x$ and $3x$. According to the problem,

$$x + 2x + 3x = 12$$

$$\Rightarrow 6x = 12 \Rightarrow x = 2$$

\therefore The largest of the numbers is $3x = 6$

07. (C) $3^n = 729 \Rightarrow 3^n = 3^6 \Rightarrow n = 6$

$$\therefore 3^{3n+1} = 3^{3(6)+1} = 3^{18+1} = 3^{19}$$

08. (B) Given $6x^2 = 1536 \text{ cm}^2$

$$a^2 = \frac{1536}{6} \text{ cm}^2 = 256 \text{ cm}^2$$

$$a^2 = (16\text{cm})^2$$

$$a = 16 \text{ cm}$$

$$\text{Volume} = a^3 = (16\text{cm})^3 = 4096 \text{ cm}^3$$

09. (C) $(x^2 - 1)(x^4 + x^2 + 1) = (x^2 - 1)[(x^2)^2 + x^2(1) + 1^2]$

$$= (x^2)^3 - 1^3 = x^6 - 1$$

10. (C) Side of square = $\sqrt{(4a^2 + 12ab + 9b^2)} \text{ cm}$

$$= \sqrt{(2a + 3b)^2} \text{ cm} = (2a + 3b) \text{ cm}$$

$$\text{Perimeter of a square} = 4s = 4(2a + 3b) \text{ cm}$$

$$= (8a + 12b) \text{ cm}$$

11. (C) Let $x = \overline{0.621} = 0.621\ 621\ 621\ \dots$

$$\therefore 1000x = 1000 \times 0.621\ 621\ 621\ \dots$$

$$1000x = 621.621\ 621\ 621\ \dots$$

$$x = \underline{0.621\ 621\ 621\ \dots}$$

$$\therefore 999x = 621$$

$$x = \frac{\overline{621}^{69\ 23}}{\underline{999}^{411\ 37}} = \frac{23}{37}$$

$$\therefore \overline{0.621} = \frac{23}{37}$$

12. (B) If $x = a + b + c$ then

$$\frac{a+b-(a+b+c)}{c} + \frac{a+c-(a+b+c)}{b}$$

$$+ \frac{c+b-(a+b+c)}{a} + \frac{4(a+b+c)}{(a+b+c)} = 1$$

$$\Rightarrow \frac{a+b-a-b-c}{c} + \frac{a+c-a-b-c}{b}$$

$$+ \frac{c+b-a-b-c}{a} + 4 = 1$$

$$\Rightarrow -\frac{c}{c} + \frac{(-b)}{b} + \frac{(-a)}{a} + 4 = 1$$

$$\Rightarrow -1 - 1 - 1 + 4 = 1$$

$$\Rightarrow 1 = 1$$

$$\text{Hence } x = (a + b + c)$$

13. (A) $(1^3 + 2^3 + 3^3 + \dots + 73^3)^{-3/2} = (1 + 8 + 27 + 64 + 125 + 216 + 343)^{-3/2}$

$$= (784)^{-3/2}$$

$$= 28^{2 \times \frac{-3}{2}}$$

$$= 28^{-3}$$

$$= \frac{1}{(28^3)}$$

$$= \frac{1}{21952}$$

14. (D)

$$\left(\frac{3}{5}x^2y - \frac{7}{3}xy^2\right)\left(\frac{3}{7}xy^2 + \frac{5}{3}x^2y\right) = \frac{3}{5}x^2y\left(\frac{3}{7}xy^2 + \frac{5}{3}x^2y\right) - \frac{7}{3}xy^2\left(\frac{3}{7}xy^2 + \frac{5}{3}x^2y\right)$$

$$= \frac{3}{5} \times \frac{3}{7} x^3 y^3 + \frac{3}{5} \times \frac{5}{3} x^4 y^2 - \frac{7}{3} \times \frac{3}{7} x^2 y^4 - \frac{7}{3} \times \frac{5}{3} x^3 y^3$$

$$= \frac{9}{35} x^3 y^3 + x^4 y^2 - x^2 y^4 - \frac{35}{9} x^3 y^3$$

$$= \frac{9}{35} x^3 y^3 - \frac{35}{9} x^3 y^3 + x^4 y^2 - x^2 y^4$$

$$\frac{81x^3y^3 - 1225x^3y^3}{315} + x^4y^2 - x^2y^4$$

$$- \frac{1144x^3y^3}{315} + x^4y^2 - x^2y^4$$

$$= x^4y^2 - \frac{1144x^3y^3}{315} - x^2y^4$$

15. (C) P = Rs. x, A = 27

r = 20% p.a.

n = 3 years.

$$\therefore y = x \left(1 + \frac{20}{100}\right)^3 \Rightarrow y = x \left(\frac{6}{5}\right)^3 \text{ s}$$

$$\Rightarrow \frac{y}{x} = \frac{216}{125}$$

16. (B) Given $\frac{a^{n+1} + b^{n+1}}{a^n + b^n} = \frac{a+b}{2}$

$$2(a^{n+1} + b^{n+1}) = (a+b)(a^n + b^n)$$

$$2a^{n+1} + 2b^{n+1} = a \times a^n + ab^n + ba^n + b \times b^n$$

$$\cancel{a^{n+1}} + a^{n+1} + b^{n+1} + \cancel{b^{n+1}} = \cancel{a^{n+1}} + ab^n + a^n b + \cancel{b^{n+1}}$$

$$\therefore a^{n+1} - a^n b = ab^n - b^{n+1}$$

$$a^n(a-b) = b^n(a-b)$$

$$a^n = b^n$$

$$\therefore n = 0 \quad [\because a \text{ \& \ } b \text{ are coprimes}]$$

(OR) Verify from options

17. (C) LHS = $x^{\frac{a+b-c}{(a-c)(b-c)}} \cdot x^{\frac{b+c-a}{(b-a)(c-a)}} \cdot x^{\frac{a+c-b}{(a-b)(c-b)}}$

$$= x^{\frac{(c-a-b)}{(c-a)(b-c)}} \cdot x^{\frac{(a-b-c)}{(c-a)(a-b)}} \cdot x^{\frac{b-c-a}{(b-c)(a-b)}}$$

$$= x^{\frac{(c-a-b)}{(c-a)(b-c)} + \frac{(a-b-c)}{(c-a)(a-b)} + \frac{b-c-a}{(b-c)(a-b)}}$$

$$= x^{\frac{(a-b)(c-a-b) + (b-c)(a-b-c) + (c-a)(b-c-a)}{(a-b)(b-c)(c-a)}}$$

$$= x^{\frac{ac-a^2-ab-bc+ab+b^2+ab-b^2-bc-ac+bc+c^2}{(a-b)(b-c)(c-a)}}$$

$$+ bc - c^2 - ac - ab + ac + a^2$$

$$= x^{\frac{0}{(a-b)(b-c)(c-a)}} = x^0 = 1$$

18. (B) Let breadth be 'x' cm

$$\text{Given } l = 3x$$

$$\text{Given } (3x - 3)(x + 5) - (3x)(x) = 57$$

$$3x^2 + 15x - 3x - 15 - 3x^2 = 57$$

$$12x = 57 + 15 = 72$$

$$x = 6$$

$$\therefore l = 3x = 18$$

$$P = 2(l + b) = 2(24 \text{ cm}) = 48 \text{ cm.}$$

19. (C) SP after 12% discount = MP $\frac{(100-12)}{100}$

$$= \text{MP} \times \frac{88}{100}$$

SP after 20%

$$\text{on above} = \text{MP} \frac{88}{100} \times \frac{(100-20)}{100}$$

$$= \text{MP} \times \frac{88}{100} \times \frac{80}{100} = \text{MP} \times \frac{88}{125}$$

Discount

$$\text{percentage} = \frac{\text{MP} - \text{MP} \left(\frac{88}{125}\right)}{\text{MP}} \times 100$$

$$= \frac{(125-88)}{125 \times \text{MP}} \times 100$$

$$= \frac{37}{5} \times 4 = \frac{148}{5} = 29 \frac{3}{5} \%$$

(OR)

$$100 - \frac{(100-d_1)(100-d_2)}{100^{n-1}}$$

$$= 100 - \frac{88 \times 80}{100} = \frac{500-352}{5} = \frac{148}{5}$$

$$\text{(OR) } a+b - \frac{ab}{100}$$

20. (B) Circumference of circle = Perimeter of a rectangle

$$2\pi r = 2(18.7 + 14.3)$$

$$\frac{22}{7} \times r = 33$$

$$r = \cancel{33}^3 \times \frac{7}{\cancel{22}_2} = \frac{21}{2} = 10.5 \text{ cm}$$

21. (A) Let $a = 20252025$, $b = 20242025$ then

$$\text{LHS} = ab - (b - 1)(a + 1)$$

$$= ab - (ab + b - a - 1)$$

$$= \cancel{ab} - \cancel{ab} - b + a + 1$$

$$= a - b + 1$$

$$= 20252025 - 20242025 + 1$$

$$= 10000 + 1$$

$$= 10001$$

22. (A) Given $\angle A + \angle C + \angle B + \angle C = 120^\circ + 140^\circ$

$$\therefore \angle A + \angle B + 2\angle C = 260^\circ$$

$$100^\circ + 2\angle C = 260^\circ \quad [\because \angle A + \angle B = 100^\circ]$$

$$2\angle C = 260^\circ - 100^\circ = 160^\circ$$

$$\angle C = \frac{160^\circ}{2} = 80^\circ$$

$$\text{But given } \therefore \angle A + \angle C = 120^\circ$$

$$\angle A + 80^\circ = 120^\circ$$

$$\angle A = 120^\circ - 80^\circ = 40^\circ$$

23. (D) $\left(\frac{1}{a^3} + \frac{1}{b^3}\right) \left(\frac{2}{a^3} - \frac{1}{a^3b^3} + \frac{2}{b^3}\right)$

$$= \frac{1}{a^3} \left(\frac{2}{a^3} - \frac{1}{a^3b^3} + \frac{2}{b^3}\right) + \frac{1}{b^3} \left(\frac{2}{a^3} - \frac{1}{a^3b^3} + \frac{2}{b^3}\right)$$

$$= \left(\begin{array}{c} \frac{1}{a^3} \times \frac{2}{a^3} - \frac{1}{a^3} \times \frac{1}{a^3b^3} + \frac{1}{a^3} \times \frac{2}{b^3} \\ + \frac{2}{a^3b^3} - \frac{1}{a^3} \times \frac{1}{b^3} + \frac{1}{b^3} \times \frac{2}{b^3} \end{array} \right)$$

$$= \left(\frac{1}{a^3} + \frac{2}{3} - \frac{2}{a^3b^3} + \frac{1}{a^3b^3} - \frac{1}{a^3b^3} + \frac{1}{b^3} + \frac{2}{3} \right)$$

$$= \frac{1+2}{a^3} + \frac{1+2}{b^3} = \frac{3}{a^3} + \frac{3}{b^3} = (a+b)$$

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24. (D) $\sqrt{(1234567)^2 - 2469133}$

$$= \sqrt{(1234567)^2 - 2469133 - 1 + 1}$$

$$= \sqrt{(1234567)^2 - 2469134 + 1}$$

$$= \sqrt{(1234567)^2 - 2(1234567)(1) + 1^2}$$

$$= \sqrt{(1234567 - 1)^2}$$

$$= 1234566$$

25. (C) $\alpha\beta = \left(\frac{-b + \sqrt{b^2 - 4ac}}{2a}\right) \left(\frac{-b - \sqrt{b^2 - 4ac}}{2a}\right)$

$$= \frac{(-b)^2 - (\sqrt{b^2 - 4ac})^2}{4a^2}$$

$$= \frac{b^2 - (b^2 - 4ac)}{4a^2} = \frac{b^2 - b^2 + 4ac}{4a^2}$$

$$= \frac{4ac}{4a^2} = \frac{c}{a}$$

26. (B) Volume of each cube

$$= (7 \text{ cm})^3 = 343 \text{ cm}^3$$

$$\therefore \text{Volume of 10 cubes} = 3,430 \text{ cm}^3$$

27. (A) Let the initial length and the breadth of the rectangle be x and y respectively.

$$\therefore \text{Initial area} = xy$$

$$\text{Now, new length} = x + x \times \frac{50}{100} = \frac{3x}{2}$$

$$\text{And new breadth} = y - y \times \frac{25}{100} = \frac{3y}{4}$$

$$\therefore \text{New area} = \frac{3x}{2} \times \frac{3y}{4} = \frac{9xy}{8}$$

Clearly, new area is more than the initial area.

\therefore Increment in percent in area

$$= \frac{\frac{9xy}{8} - xy}{xy} \times 100\% = 12.5\%$$

28. (D) If the length of the diagonals are not equal, then the quadrilateral can be a rhombus but not a square.

29. (B)

4 seat table	5 seat table	Total tables	Total people	
9	10	19	$9 \times 4 + 10 \times 5 = 86$	<input type="checkbox"/>
10	9	19	$10 \times 4 + 9 \times 5 = 85$	<input type="checkbox"/>
11	8	19	$11 \times 4 + 8 \times 5 = 84$	<input type="checkbox"/>

Hence, 8 tables can seat 5 people.

30. (B) $\frac{8^a}{2^a} = 2$, since $b \neq 0$

$$\therefore 2^{3a-a} = 2^1$$

$$\Rightarrow 2a = 1$$

$$\therefore a = \frac{1}{2}$$

MATHEMATICS - 2 (MAQ)

31. (A,B,C,D) All options are factors of the given number.

32. (A,B,C)

33. (B,C,D)

Given, $3\angle A = 4\angle B = 4\angle C = 6\angle D \dots (i)$

Let (i) = k

$$\therefore \text{we get, } \frac{k}{3} + \frac{k}{4} + \frac{k}{4} + \frac{k}{6} = 360^\circ$$

[sum of all angles of a quadrilateral = 360°]

$$\Rightarrow \frac{4k + 3k + 3k + 2k}{12} = 360^\circ$$

$$\Rightarrow k = 360^\circ$$

$$\Rightarrow k = 360^\circ$$

So, the angles are $120^\circ, 90^\circ, 90^\circ, 60^\circ$.

34. (A,C) $x^4 + 2x^2 + 9 = (x^2)^2 + 3^2 + 2x^2$
 $= (x^2)^2 + 3^2 + 2 \times x^2 \times 3 - 2x^2 \times 3 + 2x^2$
 $= (x^2 + 3)^2 - 6x^2 + 2x^2$
 $= (x^2 + 3)^2 - 4x^2$
 $= (x^2 + 3)^2 - (2x)^2$
 $= (x^2 + 2x + 3)(x^2 - 2x + 3)$

35. (A,B,D)

Given

$$x_1 y_1 = x_2 y_2 = x_3 y_3 = x_4 y_4 = x_5 y_5$$

$$12a = 6 \times 16 = 8b = 0.5c = 4d.$$

$$\therefore 12a = 16 \times 6 \Rightarrow a = 8$$

$$8b = 6 \times 16 \Rightarrow b = 12$$

$$0.5c = 6 \times 16 \Rightarrow c = 192$$

$$4d = 6 \times 16 \Rightarrow d = 24$$

REASONING

36. (D) $4 \xrightarrow{\times 2-1} 7 \xrightarrow{\times 2-1} 13 \xrightarrow{\times 2-1} 25 \xrightarrow{\times 2-1} 49 \xrightarrow{\times 2-1} 97 \xrightarrow{\times 2-1} 193$

37. (C) $(16 \times 2) + 8 = 40$; $(11 \times 2) + 5 = 27$;

$$(4 \times 2) + 11 = 19$$

38. (B) Woman — Brother

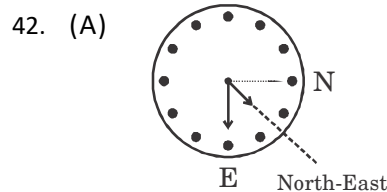


39. (C) The words given in the box are related to crop production. So, the missing word is SOW.

40. (B) Small dark fill circle is not towards the vertex, as in the other figures.

1 9 6 5 I N D O P A K

41. (A) **Т а е р и н д о в ъ к**



The hour hand points to the North-East direction.

43. (C) $\sqrt{81} + \sqrt{64} + \sqrt{144} + \sqrt{36} = 9 + 8 + 12 + 6 = 35$

$$\sqrt{49} + \sqrt{25} + \sqrt{121} + \sqrt{16} = 7 + 5 + 11 + 4 = 27$$

$$\sqrt{169} + \sqrt{625} + \sqrt{64} + \sqrt{81} = 13 + 25 + 8 + 9 = 55$$

